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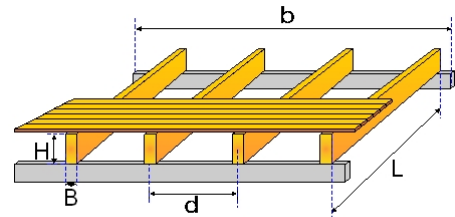
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**Examples of Floors**

**1. FLOOR-001**

Floor over one span



**1.1. General description, assumptions, materials, loads**

**1.1.1. Construction type**

Timber floor, from timber C30.  
 Spacing between floor beams 0.600m, free beam span 3.000m  
 Cross section of floor beams BxH=63mmx200mm. Floor finishing thickness 20mm

**1.1.2. Design codes**

EN1990-1-1:2002 Basis of structural design  
 EN1991-1-1:2003 Actions on structures  
 EN1995-1-1:2009 Design of timber structures

**1.1.3. Design methodology**

The internal forces are computed at the ends and the middle span of the floor beam, and the elastic deflections at midspan, for all the load combinations, according to EC 1 and EC 5. All the checks of Eurocode 5 are performed in ultimate limit state, (EC5 EN1995-1-1:2009, §6). The deflections are checked in serviceability limit state, according to EC5 EN1995-1-1:2009, §7.2. The Eurocode 5 considerations are taken into account for the check of beam vibrations (EC5 EN1995-1-1:2009, §7.3.3).

**1.1.4. Material properties (timber)** (EC5 EN1995-1-1:2009, §3)

Timber class : C30  
 Service classes : Class 1, moisture content ≤ 12% (EC5 §2.3.1.3)  
 Material factor  $\gamma_M = 1.30$  (EC5 Table 2.3)  
**Characteristic material properties for timber**  
 $f_{mk} = 30.0$  MPa,  $f_{t0k} = 18.0$  MPa,  $f_{t90k} = 0.4$  MPa  
 $f_{c0k} = 23.0$  MPa,  $f_{c90k} = 2.7$  MPa,  $f_{vk} = 4.0$  MPa  
 $E_{0m} = 12000$  MPa,  $E_{005} = 8000$  MPa,  $E_{90m} = 400$  MPa  
 $G_m = 750$  MPa,  $\rho_k = 380$  Kg/m<sup>3</sup>

**1.1.5. Distributed floor loads**

Floor finishing  $G_e = 0.500$  kN/m<sup>2</sup>  
 Self weight (insulation-beams)  $G_w = 0.100$  kN/m<sup>2</sup>  
 Ceiling under floor  $G_c = 0.300$  kN/m<sup>2</sup>  
 Sum of permanent loads  $G_e + G_w + G_c = G_s = 0.900$  kN/m<sup>2</sup>  
 Live floor load  $Q_f = 2.000$  kN/m<sup>2</sup>

**1.1.6. Line load (kN/m) on the floor beams**

Permanent load  $G_k = 0.600 \times 0.900 = 0.540$  kN/m  
 Live load  $Q_k = 0.600 \times 2.000 = 1.200$  kN/m

**1.1.7. Cross section characteristics of floor beams**

Cross section BxH=63mmx200mm,  $A = 1.260E+004$ mm<sup>2</sup>,  $I = 9.246E+007$ mm<sup>4</sup>,  $W = 4.200E+005$ mm<sup>3</sup>

**1.2. Maximum internal beam forces and deflections (L=3.000m)**

Dead loads  $G_k = 0.540$  kN/m,  $\max V = 0.81$  kN,  $\max M = 0.61$  kNm,  $\max \Delta = 0.59$  mm  
 Live loads  $Q_k = 1.200$  kN/m,  $\max V = 1.80$  kN,  $\max M = 1.35$  kNm,  $\max \Delta = 1.31$  mm

## Examples of Floors

### 1.3. Serviceability limit state (EC5 EN1995-1-1:2009, §2.2.3, §7)

#### Control of deflection in middle of beam span (EC5 §7.2)

Loading [kN/m]	u [mm]	action	$\psi_0$	$\psi_1$	$\psi_2$	Kdef
( G) Dead Gk = 0.540	0.590	Permanent	1.00	1.00	1.00	0.60
( Qf) Live Qk = 1.200	1.312	Medium-term	0.70	0.50	0.30	0.60

Load combination	w.inst	w.fin [mm]
1 G	0.590	0.945
2 Q1	1.312	1.548
3 G + Q1	1.903	2.493

$w_{fin,g} = w_{inst,g}(1+k_{def})$ ,  $w_{fin,q} = w_{inst,q}(1+\psi_2 \cdot k_{def})$  (EC5 §2.2.3, Eq.2.3, Eq.2.4)

#### Maximum deflection values

$w_{inst} = 1.903$  mm,  $w_{fin} = 2.493$  mm

#### Check according to EC5 EN1995-1-1:2009 §7.2, Tab.7.2

##### Final deflections

$w_{inst} = 1.903$  mm <  $L/300 = 3000/300 = 10.000$  mm

$w_{net,fin} = 2.493$  mm <  $L/250 = 3000/250 = 12.000$  mm

$w_{fin} = 2.493$  mm <  $L/150 = 3000/150 = 20.000$  mm

The check is satisfied

### 1.4. Vibrations (EC5 EN1995-1-1:2009, §7.3.3)

Basic floor natural frequency  $f = (3.14/2L^2) \sqrt{EI/M}$  (EC5 EN1995-1-1:2009 §7.3.3)

$L = 3.000$  m,  $E = 1.200E+010$  Nm<sup>2</sup>/m,  $I = 9.246E-005$  m<sup>4</sup>,  $M = 55.05$  kg/m<sup>2</sup>,  $f = 24.78$  Hz

$f = 24.78$  Hz > 8 Hz. The basic natural frequency is acceptable

$(EI)l/(EI)b = 10$ ,  $b/l = 6.00/3.00 = 2.00$ ,  $n_{40} = 4.00$  (EC5 Eq.7.7)

$v = 4 \times (0.4 + 0.6 \times 4.00) / (55.05 \times 6.00 \times 3.00 + 200) = 0.009$  (EC5 Eq.7.6)

$\zeta = 0.01$ ,  $v_{lim} = 6.00^{(24.78 \times 0.01 - 1)} = 0.260$ ,  $v = 0.009 \leq 0.260 = v_{lim}$  (EC5 Eq.7.4)

Requirements of EN 1995 §7.3.3 for residential floors are fulfilled

### 1.5. Ultimate limit state (EC5 EN1995-1-1:2009, §6)

Loading [kN/m]	action	$\gamma_g$	$\gamma_q$	$\psi_0$
( G) Dead Gk = 0.540	Permanent	1.35	0.00	1.00
( Qf) Live Qk = 1.200	Medium-term	0.00	1.50	0.70

L.C.	Load combination	duration class	kmod	V/Kmod	M/Kmod
1	$\gamma_g \cdot G$	Permanent	0.60	1.823	1.367
2	$\gamma_g \cdot G + \gamma_q \cdot Qf$	Medium-term	0.80	4.742	3.556
	Maximum values			4.742	3.556

#### Shear, $F_v = 3.794$ kN (EC5 §6.1.7)

Rectangular cross section,  $b_{ef} = 0.67 \times 63 = 42$  mm,  $h = 200$  mm,  $A = 8400$  mm<sup>2</sup>

Modification factor  $K_{mod} = 0.80$  (Table 3.1), material factor  $\gamma_M = 1.30$  (Table 2.3)

$f_{vk} = 4.00$  N/mm<sup>2</sup>,  $f_{vd} = K_{mod} \cdot f_{vk} / \gamma_M = 0.80 \times 4.00 / 1.30 = 2.46$  N/mm<sup>2</sup> (EC5 Eq.2.14)

$F_v = 3.794$  kN,  $v_{0d} = 1.50 F_v / A_{net} = 1000 \times 1.50 \times 3.794 / 8400 = 0.68$  N/mm<sup>2</sup> <  $2.46$  N/mm<sup>2</sup> =  $f_{vd}$  (Eq.6.13)

The check is satisfied

#### Bending, $M_{yd} = 2.845$ kNm, $M_{zd} = 0.000$ kNm (EC5 §6.1.6)

Rectangular cross section,  $b = 63$  mm,  $h = 200$  mm,  $A = 1.260E+004$  mm<sup>2</sup>,  $W_y = 4.200E+005$  mm<sup>3</sup>,  $W_z = 1.323E+005$  mm<sup>3</sup>

Modification factor  $K_{mod} = 0.80$  (Table 3.1), material factor  $\gamma_M = 1.30$  (Table 2.3)

$f_{yk} = 30.00$  N/mm<sup>2</sup>,  $f_{yd} = K_{mod} \cdot f_{yk} / \gamma_M = 0.80 \times 30.00 / 1.30 = 18.46$  N/mm<sup>2</sup>

$f_{mk} = 30.00$  N/mm<sup>2</sup>,  $f_{md} = K_{mod} \cdot f_{mk} / \gamma_M = 0.80 \times 30.00 / 1.30 = 18.46$  N/mm<sup>2</sup>

## Examples of Floors

Rectangular cross section  $K_m=0.70$  (EC5 §6.1.6.(2))  
 $\sigma_{myd} = M_{yd}/W_{my,netto} = 1E+06 \times 2.845 / 4.200E+005 = 6.77 \text{ N/mm}^2$   
 $\sigma_{mzd} = M_{zd}/W_{mz,netto} = 1E+06 \times 0.000 / 1.323E+005 = 0.00 \text{ N/mm}^2$

$\sigma_{myd}/f_{myd} + K_m \cdot \sigma_{mzd}/f_{mzd} = 0.367 + 0.000 = 0.37 < 1$  (EC5 Eq.6.11)

$K_m \cdot \sigma_{myd}/f_{myd} + \sigma_{mzd}/f_{mzd} = 0.257 + 0.000 = 0.26 < 1$  (EC5 Eq.6.12)

The check is satisfied

### Lateral torsional stability of beams, $M_{yd}=2.845 \text{ kNm}$ , $M_{zd}=0.000 \text{ kNm}$ (EC5 §6.3.3)

Rectangular cross section,  $b=63\text{mm}$ ,  $h=200\text{mm}$ ,  $A=1.260E+004\text{mm}^2$ ,  $W_y=4.200E+005\text{mm}^3$ ,  $W_z=1.323E+005\text{mm}^3$

Modification factor  $K_{mod}=0.80$  (Table 3.1), material factor  $\gamma_M=1.30$  (Table 2.3)

$f_{c0k}=23.00 \text{ N/mm}^2$ ,  $f_{c0d}=K_{mod} \cdot f_{c0k}/\gamma_M=0.80 \times 23.00 / 1.30=14.15\text{N/mm}^2$

$f_{myk}=30.00 \text{ N/mm}^2$ ,  $f_{myd}=K_{mod} \cdot f_{myk}/\gamma_M=0.80 \times 30.00 / 1.30=18.46\text{N/mm}^2$

$f_{mzk}=30.00 \text{ N/mm}^2$ ,  $f_{mzd}=K_{mod} \cdot f_{mzk}/\gamma_M=0.80 \times 30.00 / 1.30=18.46\text{N/mm}^2$

Rectangular cross section  $K_m=0.70$  (EC5 §6.1.6.(2))

$\sigma_{myd} = M_{yd}/W_{my,netto} = 1E+06 \times 2.845 / 4.200E+005 = 6.77 \text{ N/mm}^2$

$\sigma_{mzd} = M_{zd}/W_{mz,netto} = 1E+06 \times 0.000 / 1.323E+005 = 0.00 \text{ N/mm}^2$

### Buckling length $S_k$

$S_{ky} = 1.00 \times 3.000 = 3.000 \text{ m} = 3000 \text{ mm}$

$S_{kz} = 0.10 \times 3.000 = 0.300 \text{ m} = 300 \text{ mm}$

### Slenderness

$i_y = \sqrt{I_y/A} = 0.289 \times 200 = 58 \text{ mm}$ ,  $\lambda_y = 3000 / 58 = 51.72$

$i_z = \sqrt{I_z/A} = 0.289 \times 63 = 18 \text{ mm}$ ,  $\lambda_z = 300 / 18 = 16.67$

$\sigma_{m,crit} = 0.78 \cdot b^2 \cdot E_{005} / (h \cdot L_{ef}) = 0.78 \times 63^2 \times 8000 / (200 \times 2700) = 45.86\text{N/mm}^2$  (EC5 Eq.6.32)

$\sigma_{m,crit} = 0.78 \cdot b^2 \cdot E_{005} / (h \cdot L_{ef}) = 0.78 \times 200^2 \times 8000 / (63 \times 300) = 13206.35\text{N/mm}^2$  (EC5 Eq.6.32)

### Critical stresses

$\sigma_{m,crit,y} = 45.86 \text{ N/mm}^2$ ,  $\lambda_{rel,y} = \sqrt{f_{myk}/\sigma_{m,crit,y}} = 0.81$  (EC5 Eq.6.30)

$\sigma_{m,crit,z} = 13206.35 \text{ N/mm}^2$ ,  $\lambda_{rel,z} = \sqrt{f_{mzk}/\sigma_{m,crit,z}} = 0.05$  (EC5 Eq.6.30)

$\lambda_{rel,y} = 0.81$ , ( $0.75 < \lambda_{rel} \leq 1.40$ ,  $K_{crit} = 1.56 - 0.75 \lambda_{rel,m}$ ),  $K_{crit,y} = 0.95$  (EC5 Eq.6.34)

$\lambda_{rel,z} = 0.05$ , ( $\lambda_{rel} \leq 0.75$ ),  $K_{crit,z} = 1.00$  (EC5 Eq.6.34)

$\sigma_{myd} / (K_{crit,y} \cdot f_{myd}) + K_m \cdot \sigma_{mzd} / (K_{crit,z} \cdot f_{mzd}) = 0.385 + 0.000 = 0.38 < 1$  (EC5 Eq.6.33)

$K_m \cdot \sigma_{myd} / (K_{crit,y} \cdot f_{myd}) + \sigma_{mzd} / (K_{crit,z} \cdot f_{mzd}) = 0.269 + 0.000 = 0.27 < 1$  (EC5 Eq.6.33)

The check is satisfied

## 2. FLOOR-002

### Floor over two spans

#### 2.1. General description, assumptions, materials, loads

##### 2.1.1. Construction type

Timber floor, from timber C30.

Spacing between floor beams  $0.600\text{m}$ , free beam spans  $L_1=5.000\text{m}$ ,  $L_2=3.000\text{m}$

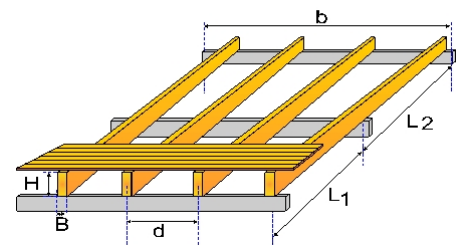
Cross section of floor beams  $B \times H=68\text{mm} \times 200\text{mm}$ . Floor finishing thickness  $25\text{mm}$

##### 2.1.2. Design codes

EN1990-1-1:2002 Basis of structural design

EN1991-1-1:2003 Actions on structures

EN1995-1-1:2009 Design of timber structures



## Examples of Floors

### 2.1.3. Design methodology

The internal forces are computed at the ends and the middle span of the floor beam, and the elastic deflections at midspan, for all the load combinations, according to EC 1 and EC 5. All the checks of Eurocode 5 are performed in ultimate limit state, (EC5 EN1995-1-1:2009, §6). The deflections are checked in serviceability limit state, according to EC5 EN1995-1-1:2009, §7.2. The Eurocode 5 considerations are taken into account for the check of beam vibrations (EC5 EN1995-1-1:2009, §7.3.3).

### 2.1.4. Material properties (timber) (EC5 EN1995-1-1:2009, §3)

Timber class : C30  
Service classes : Class 1, moisture content $\leq$ 12% (EC5 §2.3.1.3)  
Material factor  $\gamma_M=1.30$  (EC5 Table 2.3)

#### **Characteristic material properties for timber**

$f_{mk} = 30.0$  MPa,  $f_{t0k} = 18.0$  MPa,  $f_{t90k} = 0.4$  MPa  
 $f_{c0k} = 23.0$  MPa,  $f_{c90k} = 2.7$  MPa,  $f_{vk} = 4.0$  MPa  
 $E_{0m} = 12000$  MPa,  $E_{005} = 8000$  MPa,  $E_{90m} = 400$  MPa  
 $G_m = 750$  MPa,  $\rho_k = 380$  Kg/m<sup>3</sup>

### 2.1.5. Distributed floor loads

Floor finishing  $G_e = 0.500$  kN/m<sup>2</sup>  
Self weight (insulation-beams)  $G_w = 0.100$  kN/m<sup>2</sup>  
Ceiling under floor  $G_c = 0.300$  kN/m<sup>2</sup>  
Sum of permanent loads  $G_e + G_w + G_c = G_s = 0.900$  kN/m<sup>2</sup>  
Live floor load  $Q_f = 2.000$  kN/m<sup>2</sup>

### 2.1.6. Line load (kN/m) on the floor beams

Permanent load  $G_k = 0.600 \times 0.900 = 0.540$  kN/m  
Live load  $Q_k = 0.600 \times 2.000 = 1.200$  kN/m

### 2.1.7. Cross section characteristics of floor beams

Cross section  $B \times H = 68 \text{ mm} \times 200 \text{ mm}$ ,  $A = 1.360 \text{ E} + 004 \text{ mm}^2$ ,  $I = 9.751 \text{ E} + 007 \text{ mm}^4$ ,  $W = 4.533 \text{ E} + 005 \text{ mm}^3$

## 2.2. Maximum internal beam forces and deflections (L1=5.000m, L2=3.600m)

Dead loads  $G_k = 0.540$  kN/m,  $\max V = 1.62$  kN,  $\max M = 1.35$  kNm,  $\max \Delta = 1.56$  mm  
Live loads  $Q_k = 1.200$  kN/m,  $\max V = 3.60$  kN,  $\max M = 2.99$  kNm,  $\max \Delta = 5.90$  mm

## 2.3. Serviceability limit state (EC5 EN1995-1-1:2009, §2.2.3, §7)

### **Control of deflection in middle of beam span (EC5 §7.2)**

Loading [kN/m]	u [mm]	action	$\psi_0$	$\psi_1$	$\psi_2$	Kdef
( G ) Dead $G_k = 0.540$	1.563	Permanent	1.00	1.00	1.00	0.60
( Qf ) Live $Q_k = 1.200$	5.897	Medium-term	0.70	0.50	0.30	0.60

Load combination	w.inst	w.fin [mm]
1 G	1.563	2.500
2 Q1	5.897	6.958
3 G + Q1	7.459	9.458

$w_{fin,g} = w_{inst,g}(1+k_{def})$ ,  $w_{fin,q} = w_{inst,q}(1+\psi_2 \cdot k_{def})$  (EC5 §2.2.3, Eq.2.3, Eq.2.4)

### **Maximum deflection values**

$w_{inst} = 7.459$  mm,  $w_{fin} = 9.458$  mm

## Examples of Floors

### Check according to EC5 EN1995-1-1:2009 §7.2, Tab.7.2

#### Final deflections

w.inst = 7.459 mm < L/300=5000/300= 16.667 mm  
w.net,fin = 9.458 mm < L/250=5000/250= 20.000 mm  
w.fin = 9.458 mm < L/150=5000/150= 33.333 mm  
The check is satisfied

### 2.4. Vibrations (EC5 EN1995-1-1:2009, §7.3.3)

Basic floor natural frequency  $f = (3.14/2L^2) \sqrt{(EI/M)}$  (EC5 EN1995-1-1:2009 §7.3.3)  
L=5.000 m, E=1.200E+010 Nm<sup>2</sup>/m, I=9.751E-005 m<sup>4</sup>, M=55.05 kg/m<sup>2</sup>, f=9.16 Hz  
f=9.16 Hz > 8 Hz. The basic natural frequency is acceptable  
(EI)l/(EI)b=333, b/l=6.00/5.00=1.20, n40=10.57 (EC5 Eq.7.7)  
v=4x(0.4+0.6x10.57)/(55.05x6.00x5.00+200)=0.015 (EC5 Eq.7.6)  
ζ=0.01, vlim=6.00^(9.16x0.01-1)=0.196, v=0.015<=0.196=vlim (EC5 Eq.7.4)  
Requirements of EN 1995 §7.3.3 for residential floors are fulfilled

### 2.5. Ultimate limit state (EC5 EN1995-1-1:2009, §6)

Loading [kN/m]	action	γg	γq	ψo
( G) Dead Gk = 0.540	Permanent	1.35	0.00	1.00
( Qf) Live Qk = 1.200	Medium-term	0.00	1.50	0.70

L.C.	Load combination	duration class	kmod	V/Kmod	M/Kmod
1	γg.G	Permanent	0.60	3.644	3.031
2	γg.G + γq.Qf	Medium-term	0.80	9.481	7.887
	Maximum values			9.481	7.887

#### Shear, Fv=7.584 kN (EC5 §6.1.7)

Rectangular cross section, bef=0.67x68=46 mm, h=200 mm, A= 9 200 mm<sup>2</sup>  
Modification factor Kmod=0.80 (Table 3.1), material factor γM=1.30 (Table 2.3)  
fvk=4.00 N/mm<sup>2</sup>, fvd=Kmod·fvk/γM=0.80x4.00/1.30=2.46N/mm<sup>2</sup> (EC5 Eq.2.14)  
Fv=7.584 kN, rv0d=1.50Fv0d/Anetto=1000x1.50x7.584/9200=1.24N/mm<sup>2</sup> < 2.46N/mm<sup>2</sup>=fv0d (Eq.6.13)  
The check is satisfied

#### Bending, Myd=6.310 kNm, Mzd=0.000 kNm (EC5 §6.1.6)

Rectangular cross section, b=68mm, h=200mm, A=1.360E+004mm<sup>2</sup>, Wy=4.533E+005mm<sup>3</sup>, Wz=1.541E+005mm<sup>3</sup>  
Modification factor Kmod=0.80 (Table 3.1), material factor γM=1.30 (Table 2.3)  
fmyk=30.00 N/mm<sup>2</sup>, fmyd=Kmod·fmyk/γM=0.80x30.00/1.30=18.46N/mm<sup>2</sup>  
fmzk=30.00 N/mm<sup>2</sup>, fmzd=Kmod·fmzk/γM=0.80x30.00/1.30=18.46N/mm<sup>2</sup>

Rectangular cross section Km=0.70 (EC5 §6.1.6.(2))

omyd=Myd/Wmy,netto=1E+06x6.310/4.533E+005=13.92 N/mm<sup>2</sup>

omzd=Mzd/Wmz,netto=1E+06x0.000/1.541E+005= 0.00 N/mm<sup>2</sup>

omyd/fmyd+Km. omzd/fmzd=0.754+0.000= 0.75 < 1 (EC5 Eq.6.11)

Km.omyd/fmyd+omzd/fmzd=0.528+0.000= 0.53 < 1 (EC5 Eq.6.12)

The check is satisfied

#### Lateral torsional stability of beams, Myd=6.310 kNm, Mzd=0.000 kNm (EC5 §6.3.3)

Rectangular cross section, b=68mm, h=200mm, A=1.360E+004mm<sup>2</sup>, Wy=4.533E+005mm<sup>3</sup>, Wz=1.541E+005mm<sup>3</sup>  
Modification factor Kmod=0.80 (Table 3.1), material factor γM=1.30 (Table 2.3)  
fc0k=23.00 N/mm<sup>2</sup>, fc0d=Kmod·fc0k/γM=0.80x23.00/1.30=14.15N/mm<sup>2</sup>  
fmyk=30.00 N/mm<sup>2</sup>, fmyd=Kmod·fmyk/γM=0.80x30.00/1.30=18.46N/mm<sup>2</sup>  
fmzk=30.00 N/mm<sup>2</sup>, fmzd=Kmod·fmzk/γM=0.80x30.00/1.30=18.46N/mm<sup>2</sup>



## Examples of Floors

Rectangular cross section  $K_m=0.70$  (EC5 §6.1.6.(2))  
 $\sigma_{myd} = M_{yd} / W_{my, netto} = 1E+06 \times 6.310 / 4.533E+005 = 13.92 \text{ N/mm}^2$   
 $\sigma_{mzd} = M_{zd} / W_{mz, netto} = 1E+06 \times 0.000 / 1.541E+005 = 0.00 \text{ N/mm}^2$

### Buckling length $S_k$

$S_{ky} = 1.00 \times 5.000 = 5.000 \text{ m} = 5000 \text{ mm}$   
 $S_{kz} = 0.10 \times 5.000 = 0.500 \text{ m} = 500 \text{ mm}$

### Slenderness

$i_y = \sqrt{I_y / A} = 0.289 \times 200 = 58 \text{ mm}$ ,  $\lambda_y = 5000 / 58 = 86.21$   
 $i_z = \sqrt{I_z / A} = 0.289 \times 68 = 20 \text{ mm}$ ,  $\lambda_z = 500 / 20 = 25.00$

$\sigma_{m, crit} = 0.78 \cdot b^2 \cdot E_{005} / (h \cdot L_{ef}) = 0.78 \times 68^2 \times 8000 / (200 \times 4500) = 32.06 \text{ N/mm}^2$  (EC5 Eq.6.32)

$\sigma_{m, crit} = 0.78 \cdot b^2 \cdot E_{005} / (h \cdot L_{ef}) = 0.78 \times 200^2 \times 8000 / (68 \times 500) = 7341.18 \text{ N/mm}^2$  (EC5 Eq.6.32)

### Critical stresses

$\sigma_{m, crity} = 32.06 \text{ N/mm}^2$ ,  $\lambda_{rel, my} = \sqrt{f_{myk} / \sigma_{m, crity}} = 0.97$  (EC5 Eq.6.30)

$\sigma_{m, critz} = 7341.18 \text{ N/mm}^2$ ,  $\lambda_{rel, mz} = \sqrt{f_{mzk} / \sigma_{m, critz}} = 0.06$  (EC5 Eq.6.30)

$\lambda_{rel, my} = 0.97$ , ( $0.75 < \lambda_{rel} \leq 1.40$ ,  $K_{crit} = 1.56 - 0.75 \lambda_{relm}$ ),  $K_{crity} = 0.83$  (EC5 Eq.6.34)

$\lambda_{rel, mz} = 0.06$ , ( $\lambda_{rel} \leq 0.75$ ),  $K_{critz} = 1.00$  (EC5 Eq.6.34)

$\sigma_{myd} / (K_{crity} \cdot f_{myd}) + K_m \cdot \sigma_{mzd} / (K_{critz} \cdot f_{mzd}) = 0.903 + 0.000 = 0.90 < 1$  (EC5 Eq.6.33)

$K_m \cdot \sigma_{myd} / (K_{crity} \cdot f_{myd}) + \sigma_{mzd} / (K_{critz} \cdot f_{mzd}) = 0.632 + 0.000 = 0.63 < 1$  (EC5 Eq.6.33)

The check is satisfied

## 3. FLOOR-003

### Simply supported beam

#### 3.1. General description, assumptions, materials, loads

##### 3.1.1. Construction type

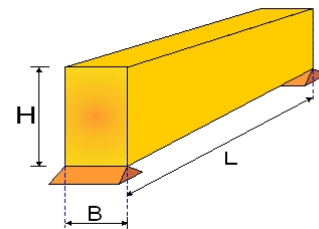
Timber floor, from timber GL24h.  
Beam free span 4.000 m  
Beam cross section  $B \times H = 100 \text{ mm} \times 200 \text{ mm}$

##### 3.1.2. Design codes

EN1990-1-1:2002 Basis of structural design  
EN1991-1-1:2003 Actions on structures  
EN1995-1-1:2009 Design of timber structures

##### 3.1.3. Design methodology

The internal forces are computed at the ends and the middle span of the floor beam, and the elastic deflections at midspan, for all the load combinations, according to EC 1 and EC 5. All the checks of Eurocode 5 are performed in ultimate limit state, (EC5 EN1995-1-1:2009, §6). The deflections are checked in serviceability limit state, according to EC5 EN1995-1-1:2009, §7.2. The Eurocode 5 considerations are taken into account for the check of beam vibrations (EC5 EN1995-1-1:2009, §7.3.3).



## Examples of Floors

### 3.1.4. Material properties (timber) (EC5 EN1995-1-1:2009, §3)

Timber class : GL24h

Service classes : Class 2, moisture content $\leq$ 20% (EC5 §2.3.1.3)

Material factor  $\gamma_M=1.25$  (EC5 Table 2.3)

#### Characteristic material properties for timber

$f_{mk} = 24.0$  MPa,  $f_{t0k} = 16.5$  MPa,  $f_{t90k} = 0.4$  MPa

$f_{c0k} = 24.0$  MPa,  $f_{c90k} = 2.7$  MPa,  $f_{vk} = 2.7$  MPa

$E_{0m} = 11600$  MPa,  $E_{005} = 9400$  MPa,  $E_{90m} = 390$  MPa

$G_m = 720$  MPa,  $\rho_k = 380$  Kg/m<sup>3</sup>

### 3.1.5. Cross section characteristics of floor beams

Cross section  $B \times H = 100 \text{ mm} \times 200 \text{ mm}$ ,  $A = 2.000 \text{ E} + 004 \text{ mm}^2$ ,  $I = 6.667 \text{ E} + 007 \text{ mm}^4$ ,  $W = 6.667 \text{ E} + 005 \text{ mm}^3$

### 3.2. Maximum internal beam forces and deflections (L=4.000m)

Dead loads  $G_k = 0.500 \text{ kN/m}$ ,  $\max V = 1.00$  kN,  $\max M = 1.00$  kNm,  $\max \Delta = 2.24$  mm

Live loads  $Q_k = 2.000 \text{ kN/m}$ ,  $\max V = 4.00$  kN,  $\max M = 4.00$  kNm,  $\max \Delta = 8.95$  mm

### 3.3. Serviceability limit state (EC5 EN1995-1-1:2009, §2.2.3, §7)

#### Control of deflection in middle of beam span (EC5 §7.2)

Loading [kN/m]	u [mm]	action	$\psi_0$	$\psi_1$	$\psi_2$	Kdef
( G) Dead $G_k = 0.500$	2.239	Permanent	1.00	1.00	1.00	0.80
( Qf) Live $Q_k = 2.000$	8.954	Medium-term	0.70	0.50	0.30	0.80

Load combination	w.inst	w.fin [mm]
1 G	2.239	4.029
2 Q1	8.954	11.103
3 G + Q1	11.193	15.132

$w_{fin,g} = w_{inst,g}(1+k_{def})$ ,  $w_{fin,q} = w_{inst,q}(1+\psi_2 \cdot k_{def})$  (EC5 §2.2.3, Eq.2.3, Eq.2.4)

#### Maximum deflection values

$w_{inst} = 11.193$  mm,  $w_{fin} = 15.132$  mm

#### Check according to EC5 EN1995-1-1:2009 §7.2, Tab.7.2

##### Final deflections

$w_{inst} = 11.193$  mm  $< L/300 = 4000/300 = 13.333$  mm

$w_{net,fin} = 15.132$  mm  $< L/250 = 4000/250 = 16.000$  mm

$w_{fin} = 15.132$  mm  $< L/150 = 4000/150 = 26.667$  mm

The check is satisfied

### 3.4. Vibrations (EC5 EN1995-1-1:2009, §7.3.3)

Basic floor natural frequency  $f = (3.14/2L^2) \sqrt{EI/M}$  (EC5 EN1995-1-1:2009 §7.3.3)

$L = 4.000$  m,  $E = 1.160 \text{ E} + 010$  Nm<sup>2</sup>/m,  $I = 6.667 \text{ E} - 005$  m<sup>4</sup>,  $M = 50.97$  kg/m<sup>2</sup>,  $f = 12.09$  Hz

$f = 12.09$  Hz  $> 8$  Hz. The basic natural frequency is acceptable

### 3.5. Ultimate limit state (EC5 EN1995-1-1:2009, §6)

Loading [kN/m]	action	$\gamma_g$	$\gamma_q$	$\psi_0$
( G) Dead $G_k = 0.500$	Permanent	1.35	0.00	1.00
( Qf) Live $Q_k = 2.000$	Medium-term	0.00	1.50	0.70

## Examples of Floors

L.C.	Load combination	duration class	kmod	V/Kmod	M/Kmod
1	yg.G	Permanent	0.60	2.250	2.250
2	yg.G + yg.Qf	Medium-term	0.80	9.188	9.188
	Maximum values			9.188	9.188

### Shear, $F_v=7.350$ kN (EC5 §6.1.7)

Rectangular cross section,  $b_{ef}=0.67 \times 100=67$  mm,  $h=200$  mm,  $A=13\,400$  mm<sup>2</sup>

Modification factor  $K_{mod}=0.80$  (Table 3.1), material factor  $\gamma_M=1.25$  (Table 2.3)

$f_{vk}=2.70$  N/mm<sup>2</sup>,  $f_{vd}=K_{mod} \cdot f_{vk} / \gamma_M = 0.80 \times 2.70 / 1.25 = 1.73$  N/mm<sup>2</sup> (EC5 Eq.2.14)

$F_v=7.350$  kN,  $\tau_{v0d}=1.50 F_{v0d} / A_{netto} = 1000 \times 1.50 \times 7.350 / 13400 = 0.82$  N/mm<sup>2</sup> <  $1.73$  N/mm<sup>2</sup> =  $f_{v0d}$  (Eq.6.13)

The check is satisfied

### Bending, $M_{yd}=7.350$ kNm, $M_{zd}=0.000$ kNm (EC5 §6.1.6)

Rectangular cross section,  $b=100$  mm,  $h=200$  mm,  $A=2.000E+004$  mm<sup>2</sup>,  $W_y=6.667E+005$  mm<sup>3</sup>,  $W_z=3.333E+005$  mm<sup>3</sup>

Modification factor  $K_{mod}=0.80$  (Table 3.1), material factor  $\gamma_M=1.25$  (Table 2.3)

$f_{yk}=24.00$  N/mm<sup>2</sup>,  $f_{mysd}=K_{mod} \cdot f_{yk} / \gamma_M = 0.80 \times 24.00 / 1.25 = 15.36$  N/mm<sup>2</sup>

$f_{mzk}=24.00$  N/mm<sup>2</sup>,  $f_{mzsd}=K_{mod} \cdot f_{mzk} / \gamma_M = 0.80 \times 24.00 / 1.25 = 15.36$  N/mm<sup>2</sup>

Rectangular cross section  $K_m=0.70$  (EC5 §6.1.6.(2))

$\sigma_{myd}=M_{yd}/W_{my,netto}=1E+06 \times 7.350 / 6.667E+005 = 11.02$  N/mm<sup>2</sup>

$\sigma_{mzd}=M_{zd}/W_{mz,netto}=1E+06 \times 0.000 / 3.333E+005 = 0.00$  N/mm<sup>2</sup>

$\sigma_{myd}/f_{mysd} + K_m \cdot \sigma_{mzd}/f_{mzsd} = 0.718 + 0.000 = 0.72 < 1$  (EC5 Eq.6.11)

$K_m \cdot \sigma_{myd}/f_{mysd} + \sigma_{mzd}/f_{mzsd} = 0.502 + 0.000 = 0.50 < 1$  (EC5 Eq.6.12)

The check is satisfied

### Lateral torsional stability of beams, $M_{yd}=7.350$ kNm, $M_{zd}=0.000$ kNm (EC5 §6.3.3)

Rectangular cross section,  $b=100$  mm,  $h=200$  mm,  $A=2.000E+004$  mm<sup>2</sup>,  $W_y=6.667E+005$  mm<sup>3</sup>,  $W_z=3.333E+005$  mm<sup>3</sup>

Modification factor  $K_{mod}=0.80$  (Table 3.1), material factor  $\gamma_M=1.25$  (Table 2.3)

$f_{c0k}=24.00$  N/mm<sup>2</sup>,  $f_{c0d}=K_{mod} \cdot f_{c0k} / \gamma_M = 0.80 \times 24.00 / 1.25 = 15.36$  N/mm<sup>2</sup>

$f_{yk}=24.00$  N/mm<sup>2</sup>,  $f_{mysd}=K_{mod} \cdot f_{yk} / \gamma_M = 0.80 \times 24.00 / 1.25 = 15.36$  N/mm<sup>2</sup>

$f_{mzk}=24.00$  N/mm<sup>2</sup>,  $f_{mzsd}=K_{mod} \cdot f_{mzk} / \gamma_M = 0.80 \times 24.00 / 1.25 = 15.36$  N/mm<sup>2</sup>

Rectangular cross section  $K_m=0.70$  (EC5 §6.1.6.(2))

$\sigma_{myd}=M_{yd}/W_{my,netto}=1E+06 \times 7.350 / 6.667E+005 = 11.02$  N/mm<sup>2</sup>

$\sigma_{mzd}=M_{zd}/W_{mz,netto}=1E+06 \times 0.000 / 3.333E+005 = 0.00$  N/mm<sup>2</sup>

### Buckling length $S_k$

$S_{ky}=1.00 \times 4.000=4.000$  m = 4000 mm

$S_{kz}=0.10 \times 4.000=0.400$  m = 400 mm

### Slenderness

$i_y = \sqrt{(I_y/A)} = 0.289 \times 200 = 58$  mm,  $\lambda_y = 4000 / 58 = 68.97$

$i_z = \sqrt{(I_z/A)} = 0.289 \times 100 = 29$  mm,  $\lambda_z = 400 / 29 = 13.79$

$\sigma_{m,crit} = M_{ycrit}/W_y = n \sqrt{(E005 \cdot I_z \cdot G005 \cdot I_{tor}) / (L_{ef} \cdot W_y)} = 84.97$  N/mm<sup>2</sup> (EC5 Eq.6.31)

$\sigma_{m,crit} = M_{ycrit}/W_y = n \sqrt{(E005 \cdot I_z \cdot G005 \cdot I_{tor}) / (L_{ef} \cdot W_y)} = 3058.81$  N/mm<sup>2</sup> (EC5 Eq.6.31)

### Critical stresses

$\sigma_{m,crit,y} = 84.97$  N/mm<sup>2</sup>,  $\lambda_{rel,my} = \sqrt{(f_{yk}/\sigma_{m,crit,y})} = 0.53$  (EC5 Eq.6.30)

$\sigma_{m,crit,z} = 3058.81$  N/mm<sup>2</sup>,  $\lambda_{rel,mz} = \sqrt{(f_{mzk}/\sigma_{m,crit,z})} = 0.09$  (EC5 Eq.6.30)

$\lambda_{rel,my}=0.53$ , ( $\lambda_{rel} \leq 0.75$ ),  $K_{crit,y}=1.00$  (EC5 Eq.6.34)

$\lambda_{rel,mz}=0.09$ , ( $\lambda_{rel} \leq 0.75$ ),  $K_{crit,z}=1.00$  (EC5 Eq.6.34)

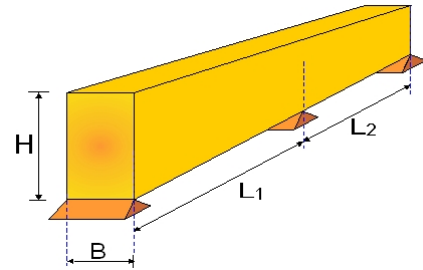
$\sigma_{myd}/(K_{crit,y} \cdot f_{mysd}) + K_m \cdot \sigma_{mzd}/(K_{crit,z} \cdot f_{mzsd}) = 0.718 + 0.000 = 0.72 < 1$  (EC5 Eq.6.33)

$K_m \cdot \sigma_{myd}/(K_{crit,y} \cdot f_{mysd}) + \sigma_{mzd}/(K_{crit,z} \cdot f_{mzsd}) = 0.502 + 0.000 = 0.50 < 1$  (EC5 Eq.6.33)

The check is satisfied

**4. FLOOR-004**

**Beam over two spans**



**4.1. General description, assumptions, materials, loads**

**4.1.1. Construction type**

Timber floor, from timber C30.  
 Free beam spans  $L_1=4.000$  m,  $L_2=3.800$  m  
 Beam cross section  $B \times H=68\text{mm} \times 200\text{mm}$

**4.1.2. Design codes**

EN1990-1-1:2002 Basis of structural design  
 EN1991-1-1:2003 Actions on structures  
 EN1995-1-1:2009 Design of timber structures

**4.1.3. Design methodology**

The internal forces are computed at the ends and the middle span of the floor beam, and the elastic deflections at midspan, for all the load combinations, according to EC 1 and EC 5. All the checks of Eurocode 5 are performed in ultimate limit state, (EC5 EN1995-1-1:2009, §6). The deflections are checked in serviceability limit state, according to EC5 EN1995-1-1:2009, §7.2. The Eurocode 5 considerations are taken into account for the check of beam vibrations (EC5 EN1995-1-1:2009, §7.3.3).

**4.1.4. Material properties (timber)** (EC5 EN1995-1-1:2009, §3)

Timber class : C30  
 Service classes : Class 1, moisture content  $\leq 12\%$  (EC5 §2.3.1.3)  
 Material factor  $\gamma_M=1.30$  (EC5 Table 2.3)

**Characteristic material properties for timber**

$f_{mk} = 30.0$  MPa,  $f_{t0k} = 18.0$  MPa,  $f_{t90k} = 0.4$  MPa  
 $f_{c0k} = 23.0$  MPa,  $f_{c90k} = 2.7$  MPa,  $f_{vk} = 4.0$  MPa  
 $E_{0m} = 12000$  MPa,  $E_{005} = 8000$  MPa,  $E_{90m} = 400$  MPa  
 $G_m = 750$  MPa,  $\rho_k = 380$  Kg/m<sup>3</sup>

**4.1.5. Cross section characteristics of floor beams**

Cross section  $B \times H=68\text{mm} \times 200\text{mm}$ ,  $A=1.360\text{E}+004\text{mm}^2$ ,  $I=4.533\text{E}+007\text{mm}^4$ ,  $W=4.533\text{E}+005\text{mm}^3$

**4.2. Maximum internal beam forces and deflections ( $L_1=4.000\text{m}$ ,  $L_2=3.800\text{m}$ )**

Dead loads  $G_k = 0.500\text{kN/m}$ ,  $\max V = 1.24$  kN,  $\max M = 0.95$  kNm,  $\max \Delta = 1.27$  mm  
 Live loads  $Q_k = 2.000\text{kN/m}$ ,  $\max V = 4.95$  kN,  $\max M = 3.81$  kNm,  $\max \Delta = 8.66$  mm

**4.3. Serviceability limit state** (EC5 EN1995-1-1:2009, §2.2.3, §7)

**Control of deflection in middle of beam span (EC5 §7.2)**

Loading [kN/m]	u [mm]	action	$\psi_0$	$\psi_1$	$\psi_2$	Kdef
( G ) Dead $G_k = 0.500$	1.275	Permanent	1.00	1.00	1.00	0.60
( Qf ) Live $Q_k = 2.000$	8.659	Medium-term	0.70	0.50	0.30	0.60

Load combination	w.inst	w.fin [mm]
1 G	1.275	2.039
2 Q1	8.659	10.217
3 G + Q1	9.933	12.257

$w_{fin,g} = w_{inst,g}(1+k_{def})$ ,  $w_{fin,q} = w_{inst,q}(1+\psi_2 \cdot k_{def})$  (EC5 §2.2.3, Eq.2.3, Eq.2.4)

## Examples of Floors

### Maximum deflection values

w.inst = 9.933 mm, w.fin = 12.257 mm

### Check according to EC5 EN1995-1-1:2009 §7.2, Tab.7.2

#### Final deflections

w.inst = 9.933 mm < L/300=4000/300= 13.333 mm

w.net,fin = 12.257 mm < L/250=4000/250= 16.000 mm

w.fin = 12.257 mm < L/150=4000/150= 26.667 mm

The check is satisfied

### 4.4. Vibrations (EC5 EN1995-1-1:2009, §7.3.3)

Basic floor natural frequency  $f = (3.14/2L^2) \sqrt{EI/M}$  (EC5 EN1995-1-1:2009 §7.3.3)

L=4.000 m, E=1.200E+010 Nm<sup>2</sup>/m, I=4.533E-005 m<sup>4</sup>, M=50.97 kg/m<sup>2</sup>, f=10.14 Hz

f=10.14 Hz > 8 Hz. The basic natural frequency is acceptable

### 4.5. Ultimate limit state (EC5 EN1995-1-1:2009, §6)

Loading [kN/m]	action	γg	γq	ψ <sub>0</sub>
( G) Dead G <sub>k</sub> = 0.500	Permanent	1.35	0.00	1.00
( Qf) Live Q <sub>k</sub> = 2.000	Medium-term	0.00	1.50	0.70

L.C.	Load combination	duration class	k <sub>mod</sub>	V/K <sub>mod</sub>	M/K <sub>mod</sub>
1	γg.G	Permanent	0.60	2.786	2.143
2	γg.G + γq.Qf	Medium-term	0.80	11.375	8.751
	Maximum values			11.375	8.751

### Shear, F<sub>v</sub>=9.100 kN (EC5 §6.1.7)

Rectangular cross section, b<sub>ef</sub>=0.67x68=46 mm, h=200 mm, A= 9 200 mm<sup>2</sup>

Modification factor K<sub>mod</sub>=0.80 (Table 3.1), material factor γ<sub>M</sub>=1.30 (Table 2.3)

f<sub>vk</sub>=4.00 N/mm<sup>2</sup>, f<sub>vd</sub>=K<sub>mod</sub>·f<sub>vk</sub>/γ<sub>M</sub>=0.80x4.00/1.30=2.46N/mm<sup>2</sup> (EC5 Eq.2.14)

F<sub>v</sub>=9.100 kN, τ<sub>v0d</sub>=1.50F<sub>v0d</sub>/A<sub>netto</sub>=1000x1.50x9.100/9200=1.48N/mm<sup>2</sup> < 2.46N/mm<sup>2</sup>=f<sub>vd</sub> (Eq.6.13)

The check is satisfied

### Bending, M<sub>yd</sub>=7.001 kNm, M<sub>zd</sub>=0.000 kNm (EC5 §6.1.6)

Rectangular cross section, b=68mm, h=200mm, A=1.360E+004mm<sup>2</sup>, W<sub>y</sub>=4.533E+005mm<sup>3</sup>, W<sub>z</sub>=1.541E+005mm<sup>3</sup>

Modification factor K<sub>mod</sub>=0.80 (Table 3.1), material factor γ<sub>M</sub>=1.30 (Table 2.3)

f<sub>yk</sub>=30.00 N/mm<sup>2</sup>, f<sub>ymd</sub>=K<sub>mod</sub>·f<sub>yk</sub>/γ<sub>M</sub>=0.80x30.00/1.30=18.46N/mm<sup>2</sup>

f<sub>mk</sub>=30.00 N/mm<sup>2</sup>, f<sub>mzd</sub>=K<sub>mod</sub>·f<sub>mk</sub>/γ<sub>M</sub>=0.80x30.00/1.30=18.46N/mm<sup>2</sup>

Rectangular cross section K<sub>m</sub>=0.70 (EC5 §6.1.6.(2))

σ<sub>yd</sub>=M<sub>yd</sub>/W<sub>my,netto</sub>=1E+06x7.001/4.533E+005=15.44 N/mm<sup>2</sup>

σ<sub>zd</sub>=M<sub>zd</sub>/W<sub>mz,netto</sub>=1E+06x0.000/1.541E+005= 0.00 N/mm<sup>2</sup>

σ<sub>yd</sub>/f<sub>ymd</sub>+K<sub>m</sub>·σ<sub>zd</sub>/f<sub>mzd</sub>=0.837+0.000= 0.84 < 1 (EC5 Eq.6.11)

K<sub>m</sub>·σ<sub>yd</sub>/f<sub>ymd</sub>+σ<sub>zd</sub>/f<sub>mzd</sub>=0.586+0.000= 0.59 < 1 (EC5 Eq.6.12)

The check is satisfied

### Lateral torsional stability of beams, M<sub>yd</sub>=7.001 kNm, M<sub>zd</sub>=0.000 kNm (EC5 §6.3.3)

Rectangular cross section, b=68mm, h=200mm, A=1.360E+004mm<sup>2</sup>, W<sub>y</sub>=4.533E+005mm<sup>3</sup>, W<sub>z</sub>=1.541E+005mm<sup>3</sup>

Modification factor K<sub>mod</sub>=0.80 (Table 3.1), material factor γ<sub>M</sub>=1.30 (Table 2.3)

f<sub>c0k</sub>=23.00 N/mm<sup>2</sup>, f<sub>c0d</sub>=K<sub>mod</sub>·f<sub>c0k</sub>/γ<sub>M</sub>=0.80x23.00/1.30=14.15N/mm<sup>2</sup>

f<sub>yk</sub>=30.00 N/mm<sup>2</sup>, f<sub>ymd</sub>=K<sub>mod</sub>·f<sub>yk</sub>/γ<sub>M</sub>=0.80x30.00/1.30=18.46N/mm<sup>2</sup>

f<sub>mk</sub>=30.00 N/mm<sup>2</sup>, f<sub>mzd</sub>=K<sub>mod</sub>·f<sub>mk</sub>/γ<sub>M</sub>=0.80x30.00/1.30=18.46N/mm<sup>2</sup>

Rectangular cross section K<sub>m</sub>=0.70 (EC5 §6.1.6.(2))

σ<sub>yd</sub>=M<sub>yd</sub>/W<sub>my,netto</sub>=1E+06x7.001/4.533E+005=15.44 N/mm<sup>2</sup>

σ<sub>zd</sub>=M<sub>zd</sub>/W<sub>mz,netto</sub>=1E+06x0.000/1.541E+005= 0.00 N/mm<sup>2</sup>

## Examples of Floors

### Buckling length $S_k$

$$S_{ky} = 1.00 \times 4.000 = 4.000 \text{ m} = 4000 \text{ mm}$$

$$S_{kz} = 0.10 \times 4.000 = 0.400 \text{ m} = 400 \text{ mm}$$

### Slenderness

$$i_y = \sqrt{I_y/A} = 0.289 \times 200 = 58 \text{ mm}, \lambda_y = 4000 / 58 = 68.97$$

$$i_z = \sqrt{I_z/A} = 0.289 \times 68 = 20 \text{ mm}, \lambda_z = 400 / 20 = 20.00$$

$$\sigma_{m,crit} = 0.78 \cdot b^2 \cdot E_{005} / (h \cdot L_{ef}) = 0.78 \times 68^2 \times 8000 / (200 \times 3600) = 40.07 \text{ N/mm}^2 \text{ (EC5 Eq.6.32)}$$

$$\sigma_{m,crit} = 0.78 \cdot b^2 \cdot E_{005} / (h \cdot L_{ef}) = 0.78 \times 200^2 \times 8000 / (68 \times 400) = 9176.47 \text{ N/mm}^2 \text{ (EC5 Eq.6.32)}$$

### Critical stresses

$$\sigma_{m,crit,y} = 40.07 \text{ N/mm}^2, \lambda_{rel,m,y} = \sqrt{f_{myk} / \sigma_{m,crit,y}} = 0.87 \text{ (EC5 Eq.6.30)}$$

$$\sigma_{m,crit,z} = 9176.47 \text{ N/mm}^2, \lambda_{rel,m,z} = \sqrt{f_{mz,k} / \sigma_{m,crit,z}} = 0.06 \text{ (EC5 Eq.6.30)}$$

$$\lambda_{rel,m,y} = 0.87, (0.75 < \lambda_{rel} \leq 1.40, K_{crit} = 1.56 - 0.75 \lambda_{rel,m}), K_{crit,y} = 0.91 \text{ (EC5 Eq.6.34)}$$

$$\lambda_{rel,m,z} = 0.06, (\lambda_{rel} \leq 0.75), K_{crit,z} = 1.00 \text{ (EC5 Eq.6.34)}$$

$$\sigma_{myd} / (K_{crit,y} \cdot f_{myd}) + K_{m,z} \cdot \sigma_{mzd} / (K_{crit,z} \cdot f_{mzd}) = 0.918 + 0.000 = 0.92 < 1 \text{ (EC5 Eq.6.33)}$$

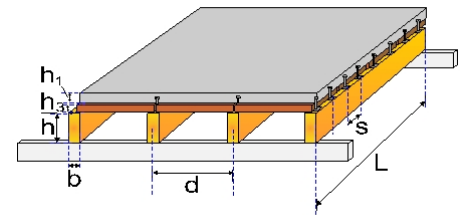
$$K_{m,y} \cdot \sigma_{myd} / (K_{crit,y} \cdot f_{myd}) + \sigma_{mzd} / (K_{crit,z} \cdot f_{mzd}) = 0.643 + 0.000 = 0.64 < 1 \text{ (EC5 Eq.6.33)}$$

The check is satisfied

## 5. FLOOR-005

### Timber-concrete composite floor

#### 5.1. General description, assumptions, materials, loads



##### 5.1.1. Construction type

Composite timber-concrete floor

Timber Class: C30

Concrete class: C25/30

Free span of floor beams :  $L = 3.600 \text{ m}$

Thickness of concrete slab :  $h_1 = 40 \text{ mm}$

Cross section of floor beams:  $B \times H = 63 \text{ mm} \times 200 \text{ mm}$

Spacing between floor beams :  $0.600 \text{ m}$

##### 5.1.2. Design codes

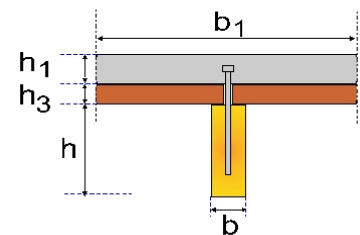
EN1990-1-1:2002 Basis of structural design

EN1991-1-1:2003 Actions on structures

EN1995-1-1:2009 Design of timber structures

EN1992-1-1:2004 Concrete structures

EN1994-1-1:2000 Composite steel and concrete structures



##### 5.1.3. Design methodology

The internal forces are computed at the ends and the middle span of the floor beam, and the elastic deflections at midspan, for all the load combinations, according to EC 1 and EC 5. All the checks of Eurocode 5 are performed in ultimate limit state, (EC5 EN1995-1-1:2009, §6). The deflections are checked in serviceability limit state, according to EC5 EN1995-1-1:2009, §7.2. The Eurocode 5 considerations are taken into account for the check of beam vibrations (EC5 EN1995-1-1:2009, §7.3.3).

The properties of the composite concrete-timber cross section are evaluated according to: EC5 EN1995-1-1:2009, Annex B

## Examples of Floors

### 5.1.4. Material properties

#### **Characteristic material properties for timber** (EC5 EN1995-1-1:2009, §3)

Timber class : C30

Service classes : Class 1, moisture content $\leq$ 12% (EN1995-1-1, §2.3.1.3)

$f_{mk} = 30.0$  MPa,  $f_{t0k} = 18.0$  MPa,  $f_{t90k} = 0.4$  MPa

$f_{c0k} = 23.0$  MPa,  $f_{c90k} = 2.7$  MPa,  $f_{vk} = 4.0$  MPa

$E_{0m} = 12000$  MPa,  $E_{005} = 8000$  MPa,  $E_{90m} = 400$  MPa

$G_m = 750$  MPa,  $\rho_k = 380$  Kg/m<sup>3</sup>

#### **Characteristic material properties for concrete** (EC2 EN1992-1-1:2004, §3.1)

Concrete class: C25/30,  $f_{ck} = 25$  N/mm<sup>2</sup>,  $f_{cm} = 2.60$  N/mm<sup>2</sup>,  $E_{cm} = 30500$  N/mm<sup>2</sup>

$f_{cd} = 0.85 \times 25 / 1.50 = 14.17$  N/mm<sup>2</sup>,  $f_{ctmd} = 0.85 \times 3 / 1.50 = 1.47$  N/mm<sup>2</sup> (EC4 EN1994-1-1:2000, §4.4.1.4)

Reinforcing steel class B500C

#### **Characteristic properties of fasteners**

Diameter of fastener=10.0 mm, Tensile strength  $f_u = 500$  N/mm<sup>2</sup>

Spacing of fasteners:  $s_{min} = 100$  mm (0-L/4, 3L/4-L),  $s_{max} = 300$  mm (L/4-3L/4)

$s_{ef} = 0.75 \times 100 + 0.25 \times 300 = 150$  mm (EC5 EN1995-1-1:2009, §9.1.3(2))

### 5.1.5. Distributed floor loads

Floor finishing  $G_e = 0.500$  kN/m<sup>2</sup>

Self weight of concrete slab  $G_b = 0.960$  kN/m<sup>2</sup>

Self weight (insulation-beams)  $G_w = 0.100$  kN/m<sup>2</sup>

Ceiling under floor  $G_c = 0.300$  kN/m<sup>2</sup>

Sum of permanent loads  $G_e + G_b + G_w + G_c = G_s = 1.860$  kN/m<sup>2</sup>

Live floor load  $Q_f = 2.000$  kN/m<sup>2</sup>

### 5.1.6. Line load (kN/m) on the floor beams

Permanent load  $G_k = 0.600 \times 1.860 = 1.116$  kN/m

Live load  $Q_k = 0.600 \times 2.000 = 1.200$  kN/m

## 5.2. Design strength of fasteners

### 5.2.1. Concrete side, (EC4 EN1994-1-1:2000, §6.3.2.1)

Shear failure,  $R_d = 0.8 f_u (\pi d^2 / 4) / \gamma_v = 25.13$  kN (EC4 EN1994-1-1:2000, Eq.6.13)

Localised compression,  $R_d = 0.23 d^2 \sqrt{f_{ck} E_{cm} / \gamma_v} = 17.96$  kN (EC4 EN1994-1-1:2000, Eq.6.14)

$d = 10.0$  mm,  $f_u = 500$  N/mm<sup>2</sup>,  $f_{ck} = 25$  N/mm<sup>2</sup>,  $E_{cm} = 30500$  N/mm<sup>2</sup>,  $\gamma_v = 1.25$

### 5.2.2. Timber side, (EC5 EN1995-1-1:2009, Eq.8.10.d)

$f_{hk} = 0.082 (1 - 0.01d) \rho_k = 28.04$  N/mm<sup>2</sup>, ( $\rho_k = 380$  kg/m<sup>3</sup>,  $d = 10.0$  mm) (EN1995-1-1 Eq.8.32)

$My_{rk} = 0.30 f_{uk} \cdot d^{2.6} = 0.30 \times 500 \times 10.0^{2.6} = 59716$  Nmm ( $f_{uk} = 500$  N/mm<sup>2</sup>) (EN1995-1-1 Eq.8.30)

$F_{vrk} = 2.30 \sqrt{My_{rk} \cdot f_{hk} \cdot d} = 9.412$  kN (EC5 EN1995-1-1:2009 Eq.8.10.d)

Load duration classes : Permanent ,  $k_{mod} = 0.60$   $R_d = K_{mod} \cdot F_{vrk} / \gamma_M = 0.60 \times 9.412 / 1.30 = 4.344$  kN

Load duration classes : Long-term ,  $k_{mod} = 0.70$   $R_d = K_{mod} \cdot F_{vrk} / \gamma_M = 0.70 \times 9.412 / 1.30 = 5.068$  kN

Load duration classes : Medium-term ,  $k_{mod} = 0.80$   $R_d = K_{mod} \cdot F_{vrk} / \gamma_M = 0.80 \times 9.412 / 1.30 = 5.792$  kN

## 5.3. Ultimate limit state (EC5 EN1995-1-1:2009, §6)

### 5.3.1. Composite cross section properties (EC5 EN1995-1-1:2009 Annex B)

Effective flange width,  $b_1 = 2L/8 = 2 \times 3600/8 = 900$  mm and  $b_1 \leq 600$  mm.  $b_1 = 600$  mm (EN1994-1-1, §2.2.21)

$K_u = (2/3) \cdot K_{ser} = (2/3) (\rho_k)^{1.5} (d/23) = (2/3) \times (380)^{1.5} \times (10/23) = 8333$  N/mm (Tab. 4.2)

Effective spacing of fastener  $s_{ef} = 150$  mm







