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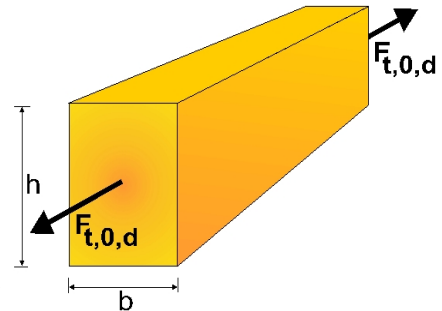
Example of ULS

1. SECT.-001

ULTIMATE LIMIT STATE, Tension
(EC5 EN1995-1-1:2009, §6.1.2)

1.1. Structural design (EC5 EN1995-1-1:2009, §6)

Material properties (EC5 EN1995-1-1:2009, §3)
Timber class : GL24h
Service classes : Class 1, moisture content ≤ 12% (§2.3.1.
Material factor $\gamma_M=1.25$ (EC5 Table 2.3)
Load duration classes : Permanent (Table 2.1)



Cross section properties (EC5 EN1995-1-1:2009, §2.4.2)
Rectangular cross section, $b=50$ mm, $h=150$ mm, $A= 7\ 500$ mm²
Timber cross section reduction 0.00%, $dA=0$ mm²
Effective timber cross section $A_{netto}= 7\ 500$ mm²

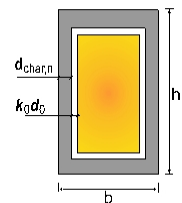
Characteristic material properties for timber (EC5 EN1995-1-1:2009, §2, §3)
Modification factor $K_{mod}=0.60$ (EC5 Table 3.1)
Material factor $\gamma_M=1.25$ (EC5 Table 2.3)
 $ft_{0k}=16.50$ N/mm², $ft_{0d}=K_{mod} \cdot ft_{0k} / \gamma_M = 0.60 \times 16.50 / 1.25 = 7.92$ N/mm² (EC5 Eq.2.14)

Cross section loads
 $F_{t0d}=10.000$ kN

Tension parallel to the grain (EC5 EN1995-1-1:2009, §6.1.2)
 $\sigma_{t0d}=F_{t0d}/A_{netto}=1000 \times 10.000 / 7500 = 1.33$ N/mm² < 7.92 N/mm² = ft_{0d} (EC5 Eq.6.1)
The check is satisfied
Percent of cross section used = 17%

1.2. Structural Fire design (EC5 EN1995-1-2:2004)

Exposure to a standard fire for 10 minutes.
Glulam GL24h with a characteristic density 380 kg/m³
The notional charring rate is $\beta_n=0.80$ mm/min (EN1995-1-2, Table 3.1)
Charring depth $d_{char,n}=\beta_n \cdot t=0.80 \times 10=8$ mm (EN1995-1-2, Eq.3.2)



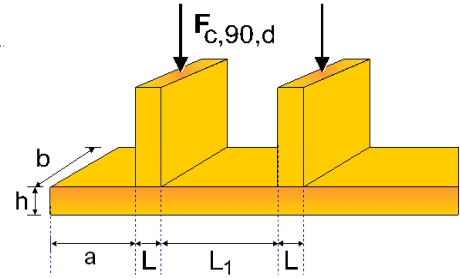
Design based on reduced cross-section method (EC5 EN1995-1-2:2004, §4.2.2)
Effective charring depth $d_{ef}=d_{char,n}+k_o \cdot d_o$, $d_o=7$ mm (EN1995-1-2, Eq.4.1)
For unprotected surfaces and $t < 20$ min, $k_o=t/20=10/20=0.50$, (EN1995-1-2, Table 4.1)
 $d_{ef}=8+0.50 \times 7=12$ mm, reduced cross section $B_f \times H_f=26 \times 126$ mm

Strength check of reduced cross-section (EC5 EN1995-1-2:2004, §2.3)
 $K_{mod,fi}=1.00$, (EN1995-1-2, §4.2.2 (5)), $\gamma_{M,fi}=1.00$ (§2.3 N. 2)
Coefficient for the 20% fractile of strength $k_{fi}=1.15$ (EN1995-1-2, Table 2.1)

Tension parallel to the grain (EC5 EN1995-1-1:2009, §6.1.2)
Rectangular cross section, $b_f=26$ mm, $h_f=126$ mm, $A=1.00 \times 26 \times 126 = 3\ 276$ mm²
 $ft_{0k}=16.50$ N/mm², $ft_{0d,fi}=K_{mod,fi} \cdot k_{fi} \cdot ft_{0k} / \gamma_{M,fi} = 1.00 \times 1.15 \times 16.50 / 1.00 = 18.98$ N/mm² (EN1995-1-2, Eq.2.1)
 $\sigma_{t0d,fi}=F_{t0d}/A_{netto}=1000 \times 10.000 / 3276 = 3.05$ N/mm² < 18.98 N/mm² = $ft_{0d,fi}$ (EC5 Eq.6.1)
The structural fire design check is satisfied

2. SECT.-002

ULTIMATE LIMIT STATE, Compression perpendicular to the grain
(EC5 EN1995-1-1:2009, §6.1.5)



Material properties (EC5 EN1995-1-1:2009, §3)
 Timber class : C24
 Service classes : Class 1, moisture content ≤ 12% (§2.3.1.
 Material factor $\gamma_M=1.30$ (EC5 Table 2.3)
 Load duration classes : Permanent (Table 2.1)

Cross section properties (EC5 EN1995-1-1:2009, §2.4.2)
 Rectangular loaded area, $b=200$ mm, $L=100$ mm, $A= 20\ 000$ mm²
 Reduction of loaded area 0.00%, $dA=0$ mm²
 Effective loaded area $A_{netto}= 20\ 000$ mm²

Characteristic material properties for timber (EC5 EN1995-1-1:2009, §2, §3)
 Modification factor $K_{mod}=0.60$ (EC5 Table 3.1)
 Material factor $\gamma_M=1.30$ (EC5 Table 2.3)
 $f_{c90k}=2.50$ N/mm², $f_{c90d}=K_{mod} \cdot f_{c90k} / \gamma_M = 0.60 \times 2.50 / 1.30 = 1.15$ N/mm² (EC5 Eq.2.14)

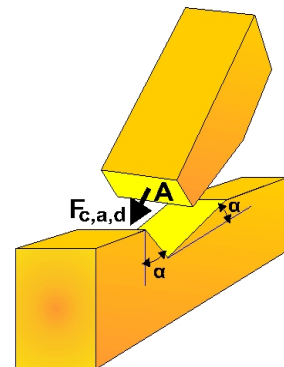
Cross section loads
 $F_{c90d}=-8.000$ kN

Compression perpendicular to the grain (EC5 EN1995-1-1:2009, §6.1.5)
 $h=100 \leq 2.50b=500$, $L=100$ mm, $L_1=150$ mm, $a=50$ mm, $L_{eff}=158$ mm, (EC5 §6.1.5.(5) Fig. 6.3)
 $K_{c90}=(2.38-L/250) \sqrt{(L_{eff}/L)} = 2.49$ (EN1995-1-1 §6.1.5.(4), Eq.6.6)
 $\sigma_{c90d}=F_{c90d}/A_{netto}=1000 \times 8.000 / 20000 = 0.40$ N/mm² < 2.87 N/mm² = $2.49 \times 1.15 = K_{c90} \times f_{c90d}$ (EN1995-1-1, Eq.6.3)
 The check is satisfied

3. SECT.-003

ULTIMATE LIMIT STATE, Compression at an angle to the grain
(EC5 EN1995-1-1:2009, §6.2.2)

3.1. Structural design (EC5 EN1995-1-1:2009, §6)



Material properties (EC5 EN1995-1-1:2009, §3)
 Timber class : C30
 Service classes : Class 1, moisture content ≤ 12% (§2.3.1.
 Material factor $\gamma_M=1.30$ (EC5 Table 2.3)
 Load duration classes : Permanent (Table 2.1)

Cross section properties (EC5 EN1995-1-1:2009, §2.4.2)
 Rectangular loaded area, $b=63$ mm, $h=100$ mm, $A= 6\ 300$ mm²
 Reduction of loaded area 0.00%, $dA=0$ mm²
 Effective loaded area $A_{netto}= 6\ 300$ mm²

Characteristic material properties for timber (EC5 EN1995-1-1:2009, §2, §3)
 Modification factor $K_{mod}=0.60$ (EC5 Table 3.1)
 Material factor $\gamma_M=1.30$ (EC5 Table 2.3)
 $f_{c0k}=23.00$ N/mm², $f_{c0d}=K_{mod} \cdot f_{c0k} / \gamma_M = 0.60 \times 23.00 / 1.30 = 10.62$ N/mm² (EC5 Eq.2.14)
 $f_{c90k}=2.70$ N/mm², $f_{c90d}=K_{mod} \cdot f_{c90k} / \gamma_M = 0.60 \times 2.70 / 1.30 = 1.25$ N/mm²

Example of ULS

Cross section loads

$F_{cad} = -9.000$ kN, at angle $\alpha = 20.00^\circ$ with the grain

Compression at an angle to the grain (EC5 EN1995-1-1:2009, §6.2.2)

$K_{c\alpha} = 1 / ((f_{c0d} / f_{c90d}) \sin^2 \alpha + \cos^2 \alpha) = 0.53$ (EC5 Eq.6.16)

$\sigma_{cad} = F_{cad} / A_{netto} = 1000 \times 9.000 / 6300 = 1.43 \text{ N/mm}^2 < 5.65 \text{ N/mm}^2 = 0.53 \times 10.62 = K_{c\alpha} \times f_{c0d}$

The check is satisfied

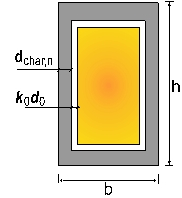
3.2. Structural Fire design (EC5 EN1995-1-2:2004)

Exposure to a standard fire for 10 minutes.

Solid timber C30 with a characteristic density 380 kg/m^3

The notional charring rate is $\beta_n = 0.80$ mm/min (EN1995-1-2, Table 3.1)

Charring depth $d_{char,n} = \beta_n \cdot t = 0.80 \times 10 = 8$ mm (EN1995-1-2, Eq.3.2)



Design based on reduced cross-section method (EC5 EN1995-1-2:2004, §4.2.2)

Effective charring depth $d_{ef} = d_{char,n} + k_o \cdot d_o$, $d_o = 7$ mm (EN1995-1-2, Eq.4.1)

For unprotected surfaces and $t < 20$ min, $k_o = t / 20 = 10 / 20 = 0.50$, (EN1995-1-2, Table 4.1)

$d_{ef} = 8 + 0.50 \times 7 = 12$ mm, reduced cross section $B_f \times H_f = 39 \times 76$ mm

Strength check of reduced cross-section (EC5 EN1995-1-2:2004, §2.3)

$K_{mod,fi} = 1.00$, (EN1995-1-2, §4.2.2 (5)), $\gamma_{M,fi} = 1.00$ (§2.3 N. 2)

Coefficient for the 20% fractile of strength $k_{fi} = 1.25$ (EN1995-1-2, Table 2.1)

Compression at an angle to the grain (EC5 EN1995-1-1:2009, §6.2.2)

Rectangular cross section, $b_f = 39$ mm, $h_f = 76$ mm, $A = 1.00 \times 39 \times 76 = 2964 \text{ mm}^2$

$f_{c0k} = 23.00 \text{ N/mm}^2$, $f_{c0d,fi} = K_{mod,fi} \cdot k_{fi} \cdot f_{c0k} / \gamma_{M,fi} = 1.00 \times 1.25 \times 23.00 / 1.00 = 28.75 \text{ N/mm}^2$ (EN1995-1-2, Eq.2.1)

$\sigma_{cad} = F_{cad} / A_{netto} = 1000 \times 9.000 / 2964 = 3.04 \text{ N/mm}^2 < 15.30 \text{ N/mm}^2 = 0.53 \times 28.75 = K_{c\alpha} \times f_{c0d,fi}$

The structural fire design check is satisfied

4. SECT.-004

ULTIMATE LIMIT STATE, Bending and tension

(EC5 EN1995-1-1:2009, §6.2.3)

4.1. Structural design (EC5 EN1995-1-1:2009, §6)

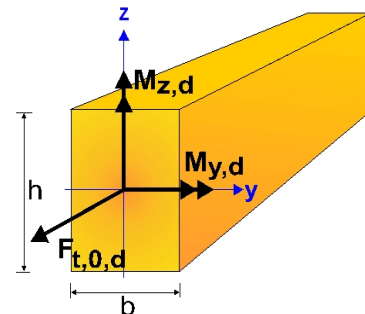
Material properties (EC5 EN1995-1-1:2009, §3)

Timber class : D40

Service classes : Class 2, moisture content $\leq 20\%$ (§2.3.1.)

Material factor $\gamma_M = 1.30$ (EC5 Table 2.3)

Load duration classes : Permanent (Table 2.1)



Cross section properties

Rectangular cross section, $b = 100$ mm, $h = 100$ mm, $A = 1.000 \text{ E} + 004 \text{ mm}^2$, $W_y = 1.667 \text{ E} + 005 \text{ mm}^3$, $W_z = 1.667 \text{ E} + 005 \text{ mm}^3$

Timber cross section reduction 0.00%, $dA = 0.000 \text{ E} + 000 \text{ mm}^2$, $dW_y = 0.000 \text{ E} + 000 \text{ mm}^3$, $dW_z = 0.000 \text{ E} + 000 \text{ mm}^3$

Effective cross section $A_{netto} = 1.000 \text{ E} + 004 \text{ mm}^2$, $W_{y,netto} = 1.667 \text{ E} + 005 \text{ mm}^3$, $W_{z,netto} = 1.667 \text{ E} + 005 \text{ mm}^3$

Characteristic material properties for timber

Modification factor $K_{mod} = 0.60$ (EC5 Table 3.1)

Material factor $\gamma_M = 1.30$ (EC5 Table 2.3)

$f_{t0k} = 24.00 \text{ N/mm}^2$, $f_{t0d} = K_{mod} \cdot f_{t0k} / \gamma_M = 0.60 \times 24.00 / 1.30 = 11.08 \text{ N/mm}^2$ (EN1995-1-1, Eq.2.14)

$f_{myk} = 40.00 \text{ N/mm}^2$, $f_{myd} = K_{mod} \cdot f_{myk} / \gamma_M = 0.60 \times 40.00 / 1.30 = 18.46 \text{ N/mm}^2$

$f_{mzk} = 40.00 \text{ N/mm}^2$, $f_{mzd} = K_{mod} \cdot f_{mzk} / \gamma_M = 0.60 \times 40.00 / 1.30 = 18.46 \text{ N/mm}^2$

Example of ULS

Cross section loads

$F_{t0d}=4.000\text{kN}$, $M_{yd}=1.000\text{kNm}$, $M_{zd}=1.000\text{kNm}$

Combined bending and axial tension (EN1995-1-1, §6.2.3)

Rectangular cross section $K_m=0.70$ (EC5 EN1995-1-1:2009 §6.1.6.(2))

$\sigma_{t0d}=F_{t0d}/A_{\text{netto}}=1000 \times 4.000/10000=0.40\text{ N/mm}^2$

$\sigma_{myd}=M_{yd}/W_{my,\text{netto}}=1\text{E}+06 \times 1.000/1.667\text{E}+005=6.00\text{ N/mm}^2$

$\sigma_{mzd}=M_{zd}/W_{mz,\text{netto}}=1\text{E}+06 \times 1.000/1.667\text{E}+005=6.00\text{ N/mm}^2$

$\sigma_{t0d}/f_{t0d}+\sigma_{myd}/f_{myd}+K_m \cdot \sigma_{mzd}/f_{mzd}=0.036+0.325+0.227=0.59 < 1$ (EN1995-1-1, Eq.6.17)

$\sigma_{t0d}/f_{t0d}+K_m \cdot \sigma_{myd}/f_{myd}+\sigma_{mzd}/f_{mzd}=0.036+0.227+0.325=0.59 < 1$ (EN1995-1-1, Eq.6.18)

The check is satisfied

Percent of cross section used =59%

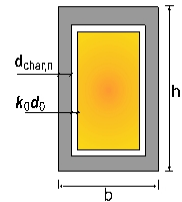
4.2. Structural Fire design (EC5 EN1995-1-2:2004)

Exposure to a standard fire for 10 minutes.

Solid Hardwood D40 with a characteristic density 550kg/m^3

The notional charring rate is $\beta_n=0.80\text{ mm/min}$ (EN1995-1-2, Table 3.1)

Charring depth $d_{\text{char},n}=\beta_n \cdot t=0.80 \times 10=8\text{ mm}$ (EN1995-1-2, Eq.3.2)



Design based on reduced cross-section method (EC5 EN1995-1-2:2004, §4.2.2)

Effective charring depth $d_{\text{ef}}=d_{\text{char},n}+k_o \cdot d_o$, $d_o=7\text{mm}$ (EN1995-1-2, Eq.4.1)

For unprotected surfaces and $t < 20\text{ min}$, $k_o=t/20=10/20=0.50$, (EN1995-1-2, Table 4.1)

$d_{\text{ef}}=8+0.50 \times 7=12\text{ mm}$, reduced cross section $B_f \times H_f=76 \times 76\text{ mm}$

Strength check of reduced cross-section (EC5 EN1995-1-2:2004, §2.3)

$K_{\text{mod},fi}=1.00$, (EN1995-1-2, §4.2.2 (5)), $\gamma_{M,fi}=1.00$ (§2.3 N. 2)

Coefficient for the 20% fractile of strength $k_{fi}=1.25$ (EN1995-1-2, Table 2.1)

Compression perpendicular to the grain (EC5 EN1995-1-1:2009, §6.1.5)

Rectangular cross section, $b_f=76\text{mm}$, $h_f=76\text{mm}$, $A=5.776\text{E}+003\text{mm}^2$, $W_y=7.316\text{E}+004\text{mm}^3$, $W_z=7.316\text{E}+004\text{mm}^3$

$f_{t0k}=24.00\text{N/mm}^2$, $f_{t0d,fi}=K_{\text{mod},fi} \cdot k_{fi} \cdot f_{t0k}/\gamma_{M,fi}=1.00 \times 1.25 \times 24.00/1.00=30.00\text{N/mm}^2$ (EN1995-1-2, Eq.2.1)

$f_{myk}=40.00\text{N/mm}^2$, $f_{myd,fi}=K_{\text{mod},fi} \cdot k_{fi} \cdot f_{myk}/\gamma_{M,fi}=1.00 \times 1.25 \times 40.00/1.00=50.00\text{N/mm}^2$ (EN1995-1-2, Eq.2.1)

$f_{mzk}=40.00\text{N/mm}^2$, $f_{mzd,fi}=K_{\text{mod},fi} \cdot k_{fi} \cdot f_{mzk}/\gamma_{M,fi}=1.00 \times 1.25 \times 40.00/1.00=50.00\text{N/mm}^2$

$\sigma_{t0d}=F_{t0d}/A_{\text{netto}}=1000 \times 4.000/5776=0.69\text{ N/mm}^2$

$\sigma_{myd}=M_{yd}/W_{my,\text{netto}}=1\text{E}+06 \times 1.000/7.316\text{E}+004=13.67\text{ N/mm}^2$

$\sigma_{mzd}=M_{zd}/W_{mz,\text{netto}}=1\text{E}+06 \times 1.000/7.316\text{E}+004=13.67\text{ N/mm}^2$

$\sigma_{t0d}/f_{t0d}+\sigma_{myd}/f_{myd,fi}+K_m \cdot \sigma_{mzd}/f_{mzd,fi}=0.023+0.273+0.191=0.49 < 1$

$\sigma_{t0d}/f_{t0d}+K_m \cdot \sigma_{myd}/f_{myd,fi}+\sigma_{mzd}/f_{mzd,fi}=0.023+0.191+0.273=0.49 < 1$

The structural fire design check is satisfied

5. SECT.-005

ULTIMATE LIMIT STATE, Lateral stability

(EC5 EN1995-1-1:2009, §6.3.3)

5.1. Structural design (EC5 EN1995-1-1:2009, §6)

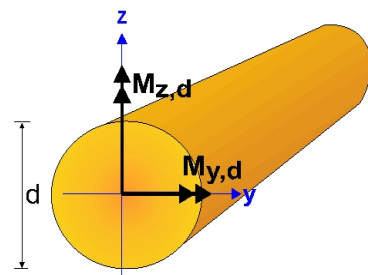
Material properties (EC5 EN1995-1-1:2009, §3)

Timber class : C24

Service classes : Class 1, moisture content $\leq 12\%$ (§2.3.1.

Material factor $\gamma_M=1.30$ (EC5 Table 2.3)

Load duration classes : Medium-term (Table 2.1)



Example of ULS

Cross section properties

Round cross section, diameter $d=150\text{mm}$, $A=1.767\text{E}+004\text{mm}^2$, $W_y=3.313\text{E}+005\text{mm}^3$, $W_z=3.313\text{E}+005\text{mm}^3$
Timber cross section reduction 0.00%, $dA=0.000\text{E}+000\text{mm}^2$, $dW_y=0.000\text{E}+000\text{mm}^3$, $dW_z=0.000\text{E}+000\text{mm}^3$
Effective cross section $A_{\text{netto}}=1.767\text{E}+004\text{mm}^2$, $W_{y,\text{netto}}=3.313\text{E}+005\text{mm}^3$, $W_{z,\text{netto}}=3.313\text{E}+005\text{mm}^3$

Characteristic material properties for timber

Modification factor $K_{\text{mod}}=0.80$ (EC5 Table 3.1)

Material factor $\gamma_M=1.30$ (EC5 Table 2.3)

$f_{c0k}=21.00\text{ N/mm}^2$, $f_{c0d}=K_{\text{mod}} \cdot f_{c0k} / \gamma_M = 0.80 \times 21.00 / 1.30 = 12.92\text{N/mm}^2$ (EN1995-1-1, Eq.2.14)

$f_{myk}=24.00\text{ N/mm}^2$, $f_{myd}=K_{\text{mod}} \cdot f_{myk} / \gamma_M = 0.80 \times 24.00 / 1.30 = 14.77\text{N/mm}^2$

$f_{mk}=24.00\text{ N/mm}^2$, $f_{mzd}=K_{\text{mod}} \cdot f_{mk} / \gamma_M = 0.80 \times 24.00 / 1.30 = 14.77\text{N/mm}^2$

Cross section loads

$M_{yd}=0.500\text{ kNm}$, $M_{zd}=0.500\text{ kNm}$

Lateral torsional stability of beams (EC5 EN1995-1-1:2009, §6.3.3)

Non rectangular cross section $K_m=1.00$ (EC5 EN1995-1-1:2009 §6.1.6.(2))

$\sigma_{myd}=M_{yd}/W_{my,\text{netto}}=1\text{E}+06 \times 0.500 / 3.313\text{E}+005 = 1.51\text{ N/mm}^2$

$\sigma_{mzd}=M_{zd}/W_{mz,\text{netto}}=1\text{E}+06 \times 0.500 / 3.313\text{E}+005 = 1.51\text{ N/mm}^2$

Buckling length S_k

$S_{ky}=1.00 \times 3.000 = 3.000\text{ m} = 3000\text{ mm}$

$S_{kz}=1.00 \times 3.000 = 3.000\text{ m} = 3000\text{ mm}$

Slenderness

$\lambda_y = \sqrt{I_y/A} = 0.250 \times 150 = 38\text{ mm}$, $\lambda_y = 3000 / 38 = 78.95$

$\lambda_z = \sqrt{I_z/A} = 0.250 \times 150 = 38\text{ mm}$, $\lambda_z = 3000 / 38 = 78.95$

$\sigma_{m,\text{crit}} = M_{ycrit}/W_y = n \sqrt{(E005 \cdot I_z \cdot G005 \cdot I_{\text{tor}}) / (L_{\text{ef}} \cdot W_y)} = 145.30\text{N/mm}^2$ (EN1995-1-1, Eq.6.31)

$\sigma_{m,\text{crit}} = M_{zcrit}/W_z = n \sqrt{(E005 \cdot I_z \cdot G005 \cdot I_{\text{tor}}) / (L_{\text{ef}} \cdot W_z)} = 145.30\text{N/mm}^2$ (EN1995-1-1, Eq.6.31)

Critical stresses

$\sigma_{m,\text{critey}} = 145.30\text{ N/mm}^2$, $\lambda_{\text{rel},my} = \sqrt{f_{myk}/\sigma_{m,\text{critey}}} = 0.41$ (EN1995-1-1, Eq.6.30)

$\sigma_{m,\text{critz}} = 145.30\text{ N/mm}^2$, $\lambda_{\text{rel},mz} = \sqrt{f_{mk}/\sigma_{m,\text{critz}}} = 0.41$ (EN1995-1-1, Eq.6.30)

$\lambda_{\text{rel},my}=0.41$, ($\lambda_{\text{rel}} \leq 0.75$), $K_{\text{critey}}=1.00$ (EN1995-1-1, Eq.6.34)

$\lambda_{\text{rel},mz}=0.41$, ($\lambda_{\text{rel}} \leq 0.75$), $K_{\text{critz}}=1.00$ (EN1995-1-1, Eq.6.34)

$\sigma_{myd} / (K_{\text{critey}} \cdot f_{myd}) + K_m \cdot \sigma_{mzd} / (K_{\text{critz}} \cdot f_{mzd}) = 0.102 + 0.102 = 0.20 < 1$ (EN1995-1-1, Eq.6.33)

$K_m \cdot \sigma_{myd} / (K_{\text{critey}} \cdot f_{myd}) + \sigma_{mzd} / (K_{\text{critz}} \cdot f_{mzd}) = 0.102 + 0.102 = 0.20 < 1$ (EN1995-1-1, Eq.6.33)

The check is satisfied

Percent of cross section used =20%

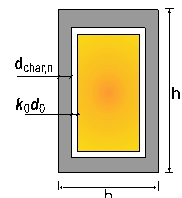
5.2. Structural Fire design (EC5 EN1995-1-2:2004)

Exposure to a standard fire for 10 minutes.

Solid timber C24 with a characteristic density 350kg/m^3

The notional charring rate is $\beta_n=0.80\text{ mm/min}$ (EN1995-1-2, Table 3.1)

Charring depth $d_{\text{char},n}=\beta_n \cdot t=0.80 \times 10=8\text{ mm}$ (EN1995-1-2, Eq.3.2)



Design based on reduced cross-section method (EC5 EN1995-1-2:2004, §4.2.2)

Effective charring depth $d_{\text{ef}}=d_{\text{char},n}+k_0 \cdot d_0$, $d_0=7\text{mm}$ (EN1995-1-2, Eq.4.1)

For unprotected surfaces and $t < 20\text{ min}$, $k_0=t/20=10/20=0.50$, (EN1995-1-2, Table 4.1)

$d_{\text{ef}}=8+0.50 \times 7=12\text{ mm}$, reduced cross section $d_f=126\text{ mm}$

Strength check of reduced cross-section (EC5 EN1995-1-2:2004, §2.3)

$K_{\text{mod},fi}=1.00$, (EN1995-1-2, §4.2.2 (5)), $\gamma_{M,fi}=1.00$ (§2.3 N. 2)

Coefficient for the 20% fractile of strength $k_{fi}=1.25$ (EN1995-1-2, Table 2.1)

Example of ULS

Lateral torsional stability of beams (EC5 EN1995-1-1:2009, §6.3.3)

Round cross section, diameter $d_f=126\text{mm}$, $A=1.247\text{E}+004\text{mm}^2$, $W_y=1.964\text{E}+005\text{mm}^3$, $W_z=1.964\text{E}+005\text{mm}^3$
 $f_{c0k}=21.00\text{N/mm}^2$, $f_{c0d}, f_i=K_{mod}, f_i \cdot K_{fi} \cdot f_{c0k} / \gamma_M, f_i=1.00 \times 1.25 \times 21.00 / 1.00=26.25\text{N/mm}^2$ (EN1995-1-2, Eq.2.1)
 $f_{yk}=24.00\text{N/mm}^2$, $f_{yd}, f_i=K_{mod}, f_i \cdot K_{fi} \cdot f_{yk} / \gamma_M, f_i=1.00 \times 1.25 \times 24.00 / 1.00=30.00\text{N/mm}^2$ (EN1995-1-2, Eq.2.1)
 $f_{mk}=24.00\text{N/mm}^2$, $f_{mzd}, f_i=K_{mod}, f_i \cdot K_{fi} \cdot f_{mk} / \gamma_M, f_i=1.00 \times 1.25 \times 24.00 / 1.00=30.00\text{N/mm}^2$
 $E_{005}=7400\text{N/mm}^2$, $E_{005}, f_i=K_{mod}, f_i \cdot K_{fi} \cdot E_{005} / \gamma_M, f_i=1.00 \times 1.25 \times 7400 / 1.00=9250\text{N/mm}^2$ (EN1995-1-2, Eq.2.2)

$\sigma_{myd}=M_{yd}/W_{my}, \text{netto}=1\text{E}+06 \times 0.500 / 1.964\text{E}+005=2.55\text{ N/mm}^2$

$\sigma_{mzd}=M_{zd}/W_{mz}, \text{netto}=1\text{E}+06 \times 0.500 / 1.964\text{E}+005=2.55\text{ N/mm}^2$

Buckling length S_k

$S_{ky}=1.00 \times 3.000=3.000\text{ m}=3000\text{ mm}$, $S_{kz}=1.00 \times 3.000=3.000\text{ m}=3000\text{ mm}$

Slenderness

$i_y=\sqrt{(I_y/A)}=0.250 \times 126=32\text{ mm}$, $\lambda_y=3000/32=93.75$

$i_z=\sqrt{(I_z/A)}=0.250 \times 126=32\text{ mm}$, $\lambda_z=3000/32=93.75$

Critical stresses

$\sigma_{m, \text{crity}}=152.56\text{ N/mm}^2$, $\lambda_{\text{rel}, my}=\sqrt{(f_{yk}/\sigma_{m, \text{crity}})}=0.44$

$\sigma_{m, \text{critz}}=152.56\text{ N/mm}^2$, $\lambda_{\text{rel}, mz}=\sqrt{(f_{mk}/\sigma_{m, \text{critz}})}=0.44$

$\lambda_{\text{rel}, my}=0.44$, ($\lambda_{\text{rel}} \leq 0.75$), $K_{\text{crity}}=1.00$

$\lambda_{\text{rel}, mz}=0.44$, ($\lambda_{\text{rel}} \leq 0.75$), $K_{\text{critz}}=1.00$

$\sigma_{myd}/(K_{\text{crity}} \cdot f_{yk}, f_i) + K_{m, \text{critz}} \cdot \sigma_{mzd}/(K_{\text{critz}} \cdot f_{mk}, f_i)=0.085+0.085=0.17 < 1$ (EN1995-1-1, Eq.6.33)

$K_{m, \text{crity}} \cdot \sigma_{myd}/(K_{\text{crity}} \cdot f_{yk}, f_i) + \sigma_{mzd}/(K_{\text{critz}} \cdot f_{mk}, f_i)=0.085+0.085=0.17 < 1$ (EN1995-1-1, Eq.6.33)

The check is satisfied

6. SECT.-006

ULTIMATE LIMIT STATE, Stability

(EC5 EN1995-1-1:2009, §6.3.2)

6.1. Structural design (EC5 EN1995-1-1:2009, §6)

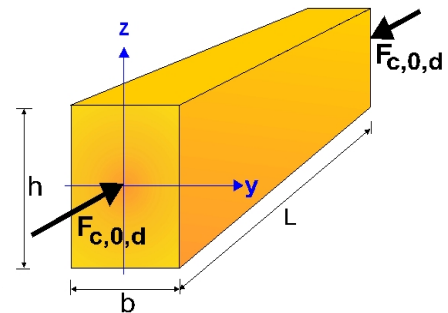
Material properties (EC5 EN1995-1-1:2009, §3)

Timber class : C30

Service classes : Class 1, moisture content $\leq 12\%$ (§2.3.1.)

Material factor $\gamma_M=1.30$ (EC5 Table 2.3)

Load duration classes : Permanent (Table 2.1)



Cross section properties

Rectangular cross section, $b=100\text{mm}$, $h=100\text{mm}$, $A=1.000\text{E}+004\text{mm}^2$, $W_y=1.667\text{E}+005\text{mm}^3$, $W_z=1.667\text{E}+005\text{mm}^3$

Timber cross section reduction 0.00%, $dA=0.000\text{E}+000\text{mm}^2$, $dW_y=0.000\text{E}+000\text{mm}^3$, $dW_z=0.000\text{E}+000\text{mm}^3$

Effective cross section $A_{\text{netto}}=1.000\text{E}+004\text{mm}^2$, $W_{y, \text{netto}}=1.667\text{E}+005\text{mm}^3$, $W_{z, \text{netto}}=1.667\text{E}+005\text{mm}^3$

Characteristic material properties for timber

Modification factor $K_{mod}=0.60$ (EC5 Table 3.1)

Material factor $\gamma_M=1.30$ (EC5 Table 2.3)

$E_{005}=8000\text{N/mm}^2$

$f_{c0k}=23.00\text{ N/mm}^2$, $f_{c0d}=K_{mod} \cdot f_{c0k} / \gamma_M=0.60 \times 23.00 / 1.30=10.62\text{N/mm}^2$ (EN1995-1-1, Eq.2.14)

$f_{yk}=30.00\text{ N/mm}^2$, $f_{yd}=K_{mod} \cdot f_{yk} / \gamma_M=0.60 \times 30.00 / 1.30=13.85\text{N/mm}^2$

$f_{mk}=30.00\text{ N/mm}^2$, $f_{mzd}=K_{mod} \cdot f_{mk} / \gamma_M=0.60 \times 30.00 / 1.30=13.85\text{N/mm}^2$

Cross section loads

$F_{c0d}=-5.000\text{ kN}$

Example of ULS

Column stability (EC5 EN1995-1-1:2009, §6.3.2)

Rectangular cross section $K_m=0.70$ (EC5 EN1995-1-1:2009 §6.1.6.(2))

$$\sigma_{c0d} = F_{c0d} / A_{netto} = 1000 \times 5.000 / 10000 = 0.50 \text{ N/mm}^2$$

Buckling length S_k

$$S_{ky} = 2.00 \times 3.600 = 7.200 \text{ m} = 7200 \text{ mm}$$

$$S_{kz} = 2.00 \times 3.600 = 7.200 \text{ m} = 7200 \text{ mm}$$

Slenderness

$$i_y = \sqrt{I_y / A} = 0.289 \times 100 = 29 \text{ mm}, \lambda_y = 7200 / 29 = 248.28$$

$$i_z = \sqrt{I_z / A} = 0.289 \times 100 = 29 \text{ mm}, \lambda_z = 7200 / 29 = 248.28$$

Critical stresses

$$\sigma_{c,crity} = n^2 E_{005} / \lambda_y^2 = 1.28 \text{ N/mm}^2, \lambda_{rel,y} = \sqrt{f_{c0k} / \sigma_{c,crity}} = 4.24 \text{ (EN1995-1-1, Eq.6.21)}$$

$$\sigma_{c,critz} = n^2 E_{005} / \lambda_z^2 = 1.28 \text{ N/mm}^2, \lambda_{rel,z} = \sqrt{f_{c0k} / \sigma_{c,critz}} = 4.24 \text{ (EN1995-1-1, Eq.6.22)}$$

$\beta_c = 0.20$ (solid timber)

$$k_y = 0.5 [1 + \beta_c (\lambda_{rel,y} - 0.3) + \lambda_{rel,y}^2] = 9.87, K_{cy} = 1 / (k_y + \sqrt{k_y^2 - \lambda_{rel,y}^2}) = 0.053 \text{ (Eq.6.27 6.25)}$$

$$k_z = 0.5 [1 + \beta_c (\lambda_{rel,z} - 0.3) + \lambda_{rel,z}^2] = 9.87, K_{cz} = 1 / (k_z + \sqrt{k_z^2 - \lambda_{rel,z}^2}) = 0.053 \text{ (Eq.6.28 6.26)}$$

$$\sigma_{c0d} / (K_{cy} \cdot f_{c0d}) = 0.89 < 1 \text{ (EN1995-1-1, Eq.6.23)}$$

$$\sigma_{c0d} / (K_{cz} \cdot f_{c0d}) = 0.89 < 1 \text{ (EN1995-1-1, Eq.6.24)}$$

The check is satisfied

Percent of cross section used = 89%

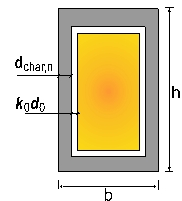
6.2. Structural Fire design (EC5 EN1995-1-2:2004)

Exposure to a standard fire for 10 minutes.

Solid timber C30 with a characteristic density 380 kg/m^3

The notional charring rate is $\beta_n = 0.80 \text{ mm/min}$ (EN1995-1-2, Table 3.1)

$$\text{Charring depth } d_{char,n} = \beta_n \cdot t = 0.80 \times 10 = 8 \text{ mm (EN1995-1-2, Eq.3.2)}$$



Design based on reduced cross-section method (EC5 EN1995-1-2:2004, §4.2.2)

Effective charring depth $d_{ef} = d_{char,n} + k_0 \cdot d_0$, $d_0 = 7 \text{ mm}$ (EN1995-1-2, Eq.4.1)

For unprotected surfaces and $t < 20 \text{ min}$, $k_0 = t / 20 = 10 / 20 = 0.50$, (EN1995-1-2, Table 4.1)

$$d_{ef} = 8 + 0.50 \times 7 = 12 \text{ mm, reduced cross section } B_f \times H_f = 76 \times 76 \text{ mm}$$

Strength check of reduced cross-section (EC5 EN1995-1-2:2004, §2.3)

$K_{mod,fi} = 1.00$, (EN1995-1-2, §4.2.2 (5)), $\gamma_{M,fi} = 1.00$ (§2.3 N. 2)

Coefficient for the 20% fractile of strength $k_{fi} = 1.25$ (EN1995-1-2, Table 2.1)

Column stability (EC5 EN1995-1-1:2009, §6.3.2)

Rectangular cross section, $b_f = 76 \text{ mm}$, $h_f = 76 \text{ mm}$, $A = 5.776 \text{ E}+003 \text{ mm}^2$, $W_y = 7.316 \text{ E}+004 \text{ mm}^3$, $W_z = 7.316 \text{ E}+004 \text{ mm}^3$

$$f_{c0k} = 23.00 \text{ N/mm}^2, f_{c0d,fi} = K_{mod,fi} \cdot k_{fi} \cdot f_{c0k} / \gamma_{M,fi} = 1.00 \times 1.25 \times 23.00 / 1.00 = 28.75 \text{ N/mm}^2 \text{ (EN1995-1-2, Eq.2.1)}$$

$$f_{myk} = 30.00 \text{ N/mm}^2, f_{myd,fi} = K_{mod,fi} \cdot k_{fi} \cdot f_{myk} / \gamma_{M,fi} = 1.00 \times 1.25 \times 30.00 / 1.00 = 37.50 \text{ N/mm}^2 \text{ (EN1995-1-2, Eq.2.1)}$$

$$f_{mzk} = 30.00 \text{ N/mm}^2, f_{mzd,fi} = K_{mod,fi} \cdot k_{fi} \cdot f_{mzk} / \gamma_{M,fi} = 1.00 \times 1.25 \times 30.00 / 1.00 = 37.50 \text{ N/mm}^2$$

$$E_{005} = 8000 \text{ N/mm}^2, E_{005,fi} = K_{mod,fi} \cdot k_{fi} \cdot E_{005} / \gamma_{M,fi} = 1.00 \times 1.25 \times 8000 / 1.00 = 10000 \text{ N/mm}^2 \text{ (EN1995-1-2, Eq.2.2)}$$

$$\sigma_{c0d} = F_{c0d} / A_{netto} = 1000 \times 5.000 / 5776 = 0.87 \text{ N/mm}^2$$

Buckling length S_k

$$S_{ky} = 2.00 \times 3.600 = 7.200 \text{ m}, S_{kz} = 2.00 \times 3.600 = 7.200 \text{ m} = 7200 \text{ mm}$$

Slenderness

$$i_y = \sqrt{I_y / A} = 0.289 \times 76 = 22 \text{ mm}, \lambda_y = 7200 / 22 = 327.27$$

$$i_z = \sqrt{I_z / A} = 0.289 \times 76 = 22 \text{ mm}, \lambda_z = 7200 / 22 = 327.27$$

Example of ULS

Critical stresses

$$\begin{aligned}\sigma_{c,crity} &= \pi^2 E 005 / \lambda y^2 = 0.92 \text{ N/mm}^2, \lambda_{rel,y} = \sqrt{(f_{c0d,fi} / \sigma_{c,crity})} = 5.00 \\ \sigma_{c,critz} &= \pi^2 E 005 / \lambda z^2 = 0.92 \text{ N/mm}^2, \lambda_{rel,z} = \sqrt{(f_{c0d,fi} / \sigma_{c,critz})} = 5.00\end{aligned}$$

$\beta_c = 0.20$ (solid timber)

$$\begin{aligned}k_y &= 0.5 [1 + \beta_c (\lambda_{rel,y} - 0.3) + \lambda_{rel,y}^2] = 13.45, K_{cy} = 1 / (k_y + \sqrt{(k_y^2 - \lambda_{rel,y}^2)}) = 0.039 \\ k_z &= 0.5 [1 + \beta_c (\lambda_{rel,z} - 0.3) + \lambda_{rel,z}^2] = 13.45, K_{cz} = 1 / (k_z + \sqrt{(k_z^2 - \lambda_{rel,z}^2)}) = 0.039\end{aligned}$$

$$\sigma_{c0d} / (K_{cy} \cdot f_{c0d,fi}) = 0.77 < 1 \quad (\text{EN1995-1-1, Eq.6.23})$$

$$\sigma_{c0d} / (K_{cz} \cdot f_{c0d,fi}) = 0.77 < 1 \quad (\text{EN1995-1-1, Eq.6.24})$$

The check is satisfied
